

# Lecture 8

## Photodetectors

EE 440 – Photonic systems and technology  
*Spring 2025*

# Basic operation principle

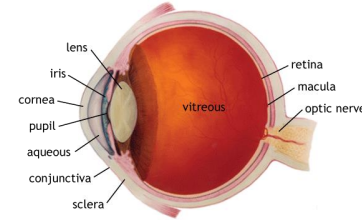
# Photodetector

Photodetectors convert light (power) into an electrical signal (photocurrent)

- Uses the photoelectric effect.

The eye is a photodetector:

- Spectral response is limited to wavelength of  $0.4\ \mu\text{m}$  to  $0.7\ \mu\text{m}$



For telecommunication need:

- Good sensitivity (responsivity) at the desired wavelength of operation.
- Fast response to be able to handle high speed data.
- Low noise to avoid distortions to the signal.
- Compatible physical dimensions with the entire systems
- Long operating life and reasonable cost

Only **photodiodes** are used in optical communication systems

# Photodiode basics

All detectors for optical communication use **optical absorption** in a **depletion region**.

- Light absorption occurs when energy of incident photons exceeds bandgap energy

$$\textit{Photon energy } h\nu > \textit{Bandgap energy}$$

- Convert photons to electron-hole pairs .
- Can then sense the number of electron-hole pairs generated.

A voltage applied across the device sets an electric field in the depletion region: electron-hole pairs give rise to a measurable photocurrent  $i_p$

- The figure of merit of the photodiode is the responsivity  $R$  (in A/W) defined as:

$$i_p = RP_{in}$$

# Quantum efficiency

Responsivity of a photodiode can be expressed in terms of the diode's *quantum efficiency*  $\eta$

$$\eta = \frac{\# \text{ electrons from photocurrent generation}}{\# \text{ photons incident}}$$

$$\eta = \frac{i_p / q}{P_{in} / h\nu} = \frac{h\nu}{q} \frac{i_p}{P_{in}} = \frac{h\nu}{q} R$$

With  $q$  = electronic charge

Rewrite responsivity:

$$R = \frac{\eta q}{h\nu}$$

$$R \approx \frac{\eta \lambda}{1.24}, \lambda \text{ in } \mu\text{m}$$

Responsivity

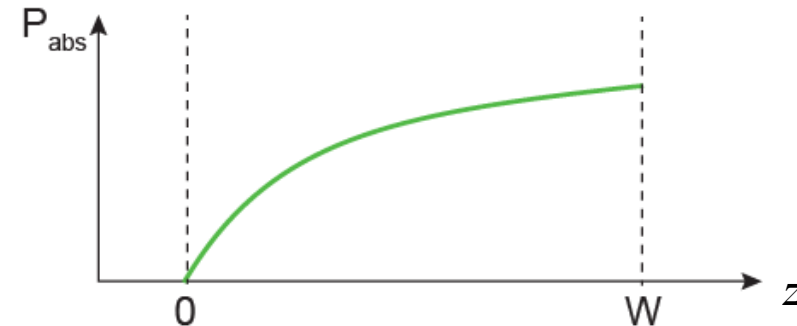
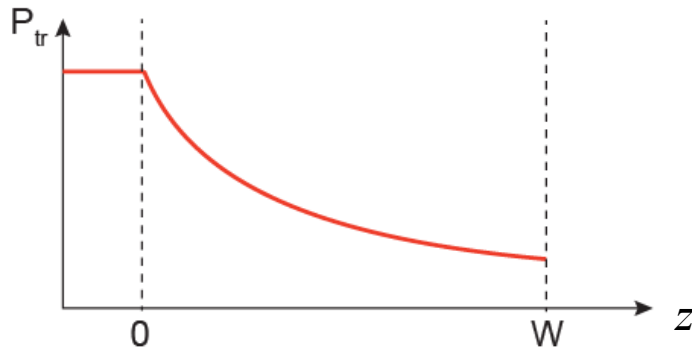
# Absorption coefficient

As the photon flux goes through the semiconductor of thickness  $W$ , it will be absorbed as it progresses through the material.

- Given absorption coefficient  $\alpha$ , transmitted ( $P_{tr}$ ) and absorbed powers ( $P_{abs}$ ) are:

$$P_{tr}(z) = P_{in} \exp(-\alpha z)$$

$$P_{abs}(z) = P_{in} - P_{tr}(z) = P_{in}[1 - \exp(-\alpha z)]$$



# Quantum efficiency

Since each absorbed photon creates an electron-hole pair we define an absorption quantum efficiency:

$$\eta_{abs} = \frac{P_{abs}(W)}{P_{in}(W)} = 1 - \exp(-\alpha W)$$

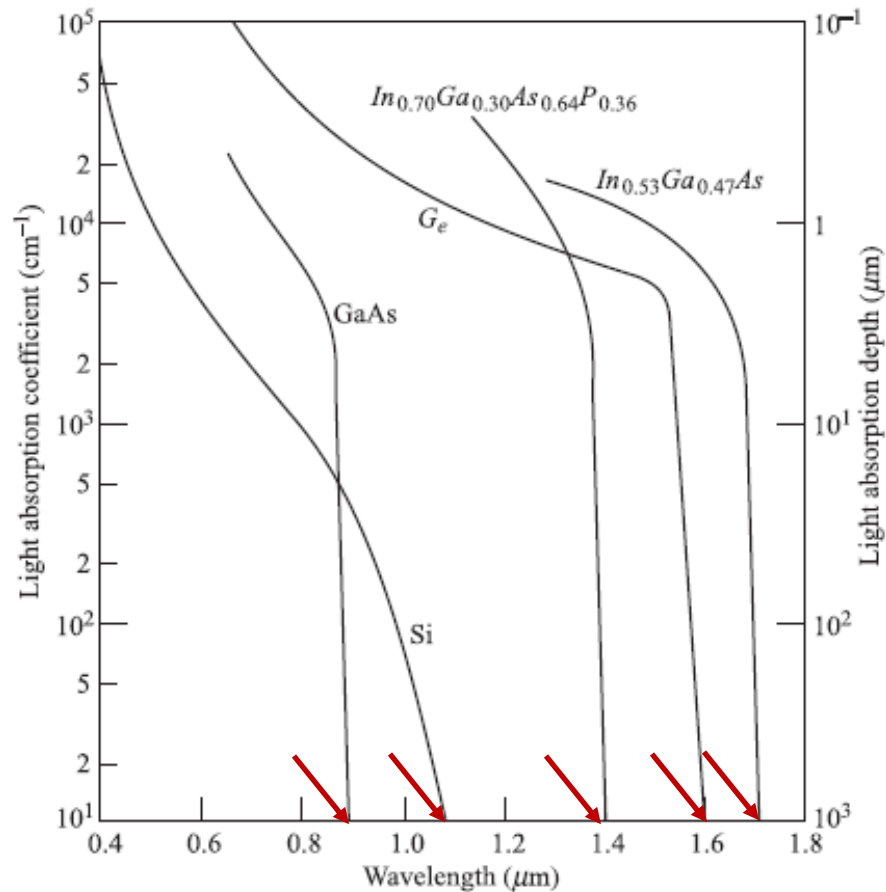
Photodiodes also have an internal quantum efficiency  $\eta_{int}$

- Not all electron-hole pairs will contribute to the photocurrent.

The quantum efficiency is therefore given by:

$$\eta = \eta_{int}\eta_{abs} = \eta_{int}[1 - \exp(-\alpha W)]$$

# Absorption coefficient $\alpha$



Large values of  $\alpha$  ( $10^4$  cm $^{-1}$ ) can be realized in most semiconductors

Photodetectors can be made of indirect bandgap semiconductor (Si, Ge)

- Absorption edge is not as sharp

Absorption becomes tends to zero at the cut-off wavelength  $\lambda_c$

$$\lambda_c = \frac{hc}{E_g}$$



## Example

A photodiode has a quantum efficiency of 50% at a wavelength of 900 nm.

What is its responsivity at 900 nm ?

What is the optical power if the mean photocurrent is 10  $\mu\text{A}$ ?

Given that the absorption is  $10^3 \text{ cm}^{-1}$ , and assume 100% internal quantum efficiency, what is the length of the active medium ?

# Types of photodiodes

# Photodiode types

## p-n photodiodes

- Electron-hole pairs created in the depletion region of a p-n junction in proportion to the optical power
- Electrons and holes are swept out by the electric field leading to a current (in photoconductive mode)

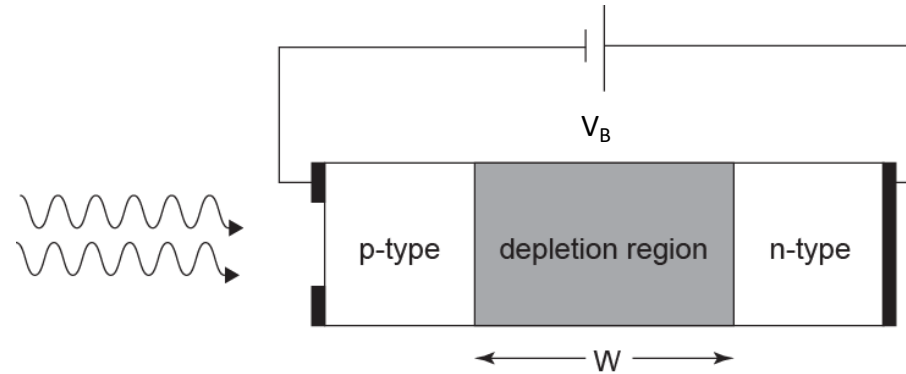
## p-i-n photodiodes

- Electric field is concentrated in an intrinsic (i) layer

## Avalanche photodiodes (APD)

- Like p-i-n photodiodes but have an additional layer
- An average of  $M$  secondary electron-hole pairs are generated through impact ionization for each primary pair

A p-n photodiode is a p-n junction whose reverse current increases when it absorbs photon



Photons are absorbed everywhere with absorption coefficient  $\alpha$ , resulting in electron-hole pairs

Under an electric field the generated charge carriers can be transported

- For a p-n junction, electric field is only in the depletion region
- The depletion region is therefore where it is desirable to generate photo-carriers.

# Bias of p-n photodiode

As an electronic device, the photodiode under illumination has an  $i - V$  relation given by:

$$i = i_0 \left[ \exp \left( \frac{qV}{k_B T} \right) - 1 \right] - i_p$$

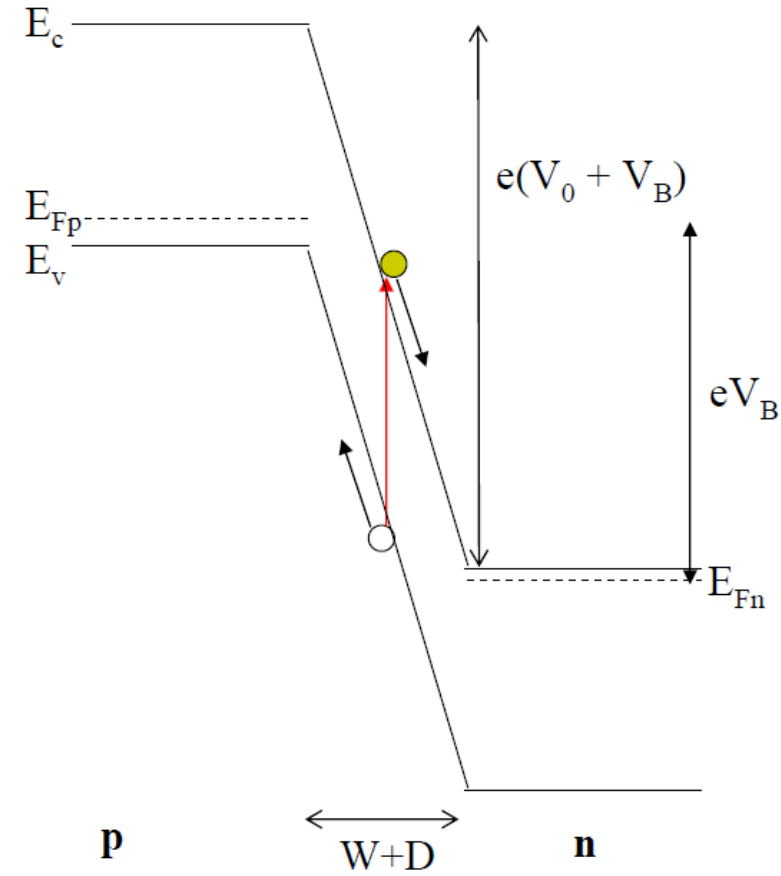
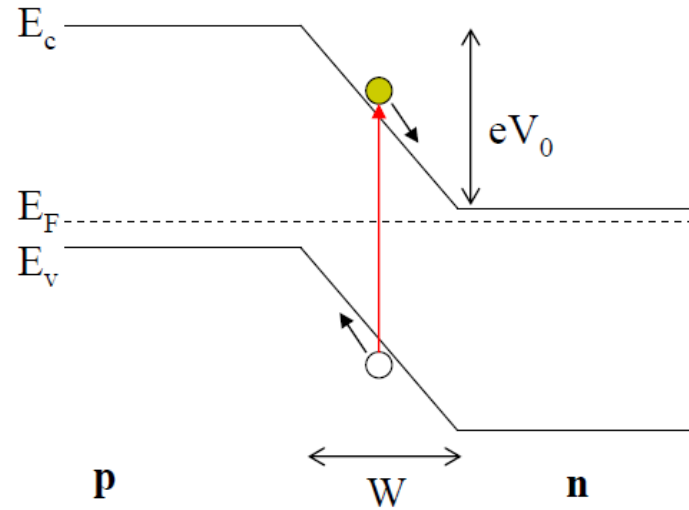
$i$ : is the injection current under a forward bias  $V$

$i_0$ : is the dark current representing thermal generated free carrier which flow through the junction

There are two modes of operation for a junction photodiode

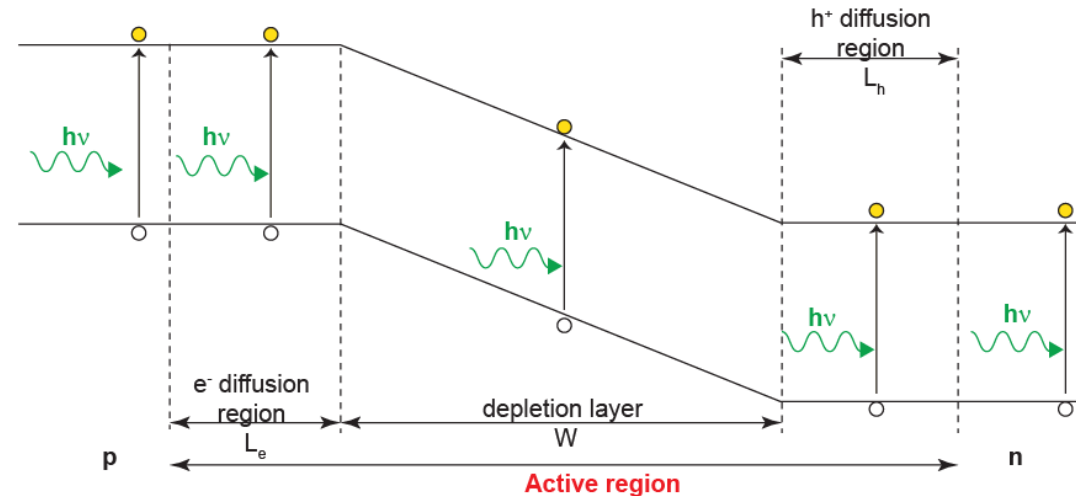
- Photoconductive mode – including short circuit condition (current source)
- Photovoltaic mode – including open circuit condition (voltage source)

# Reverse bias p-n junction



# Reverse biased mode: photoconductive

$e^-$ - $h$  pairs can be generated in *3 possible locations*



## Depletion region

Charges quickly drift in opposite directions under influence of strong  $E$  field and *contribute* to the reverse photocurrent  $i_p$

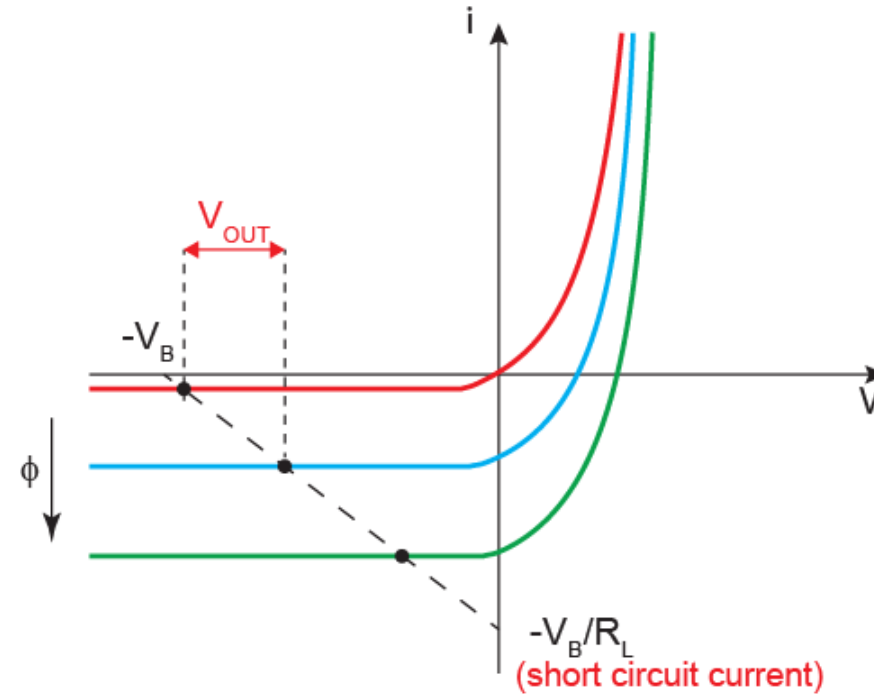
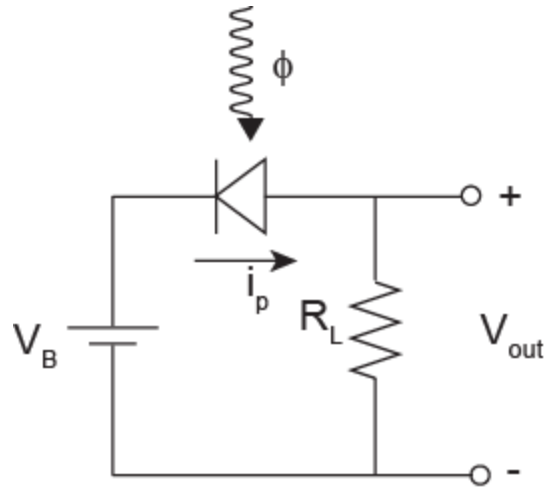
## Away from depletion region

Charged cannot be transported (no  $E$  field): wander until recombined, not contributing to the photocurrent  $i_p$

## Vicinity of depletion region

Charges can enter depletion region by random diffusion and then *contribute* to the reverse photocurrent  $i_p$

# Reverse biased mode: photoconductive



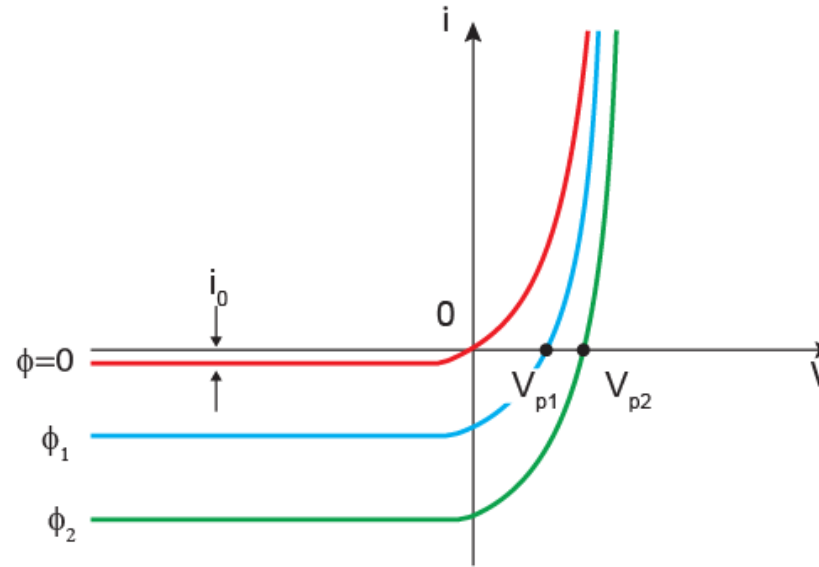
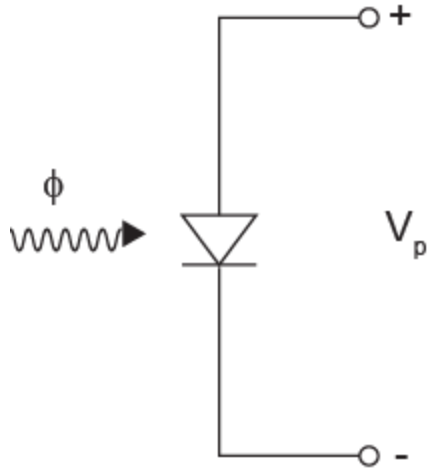
Load resistor  $R_L$  is inserted in the circuit

- $R_L < R_i$  , the internal resistance of the junction
- Keep  $V_{out} < V_B$  so that the diode remains reversed biased

Have  $V_{out} = (i_0 + i_p)R_L$



# Open circuit mode: photovoltaic



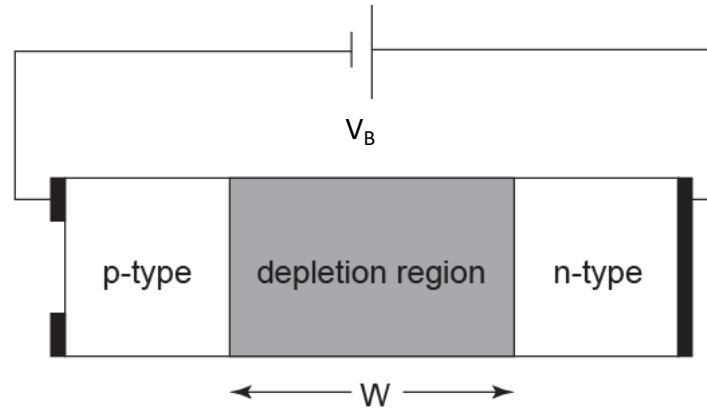
Light generates  $e^-$ - $h$  pairs in depletion region

- Photogenerated majority carriers *forward bias* the junction
- Net result: *photovoltage*  $V_p$  across the device

Limit on  $V_p$  is the equilibrium contact potential  $V_0$  as drift current vanishes with  $V_p = V_0$

Note: responsivity for such device is measured in V/W rather than A/W

# Limits of p-n photodiodes



Problem with p-n photodiode is the limited width of depletion region:

- Leads to the presence of a diffusive component in the photocurrent.
- Diffusion is slow process ( $> \text{ns}$  to diffuse  $1\mu\text{m}$ ): distorts response of photodiode.

Optical pulse



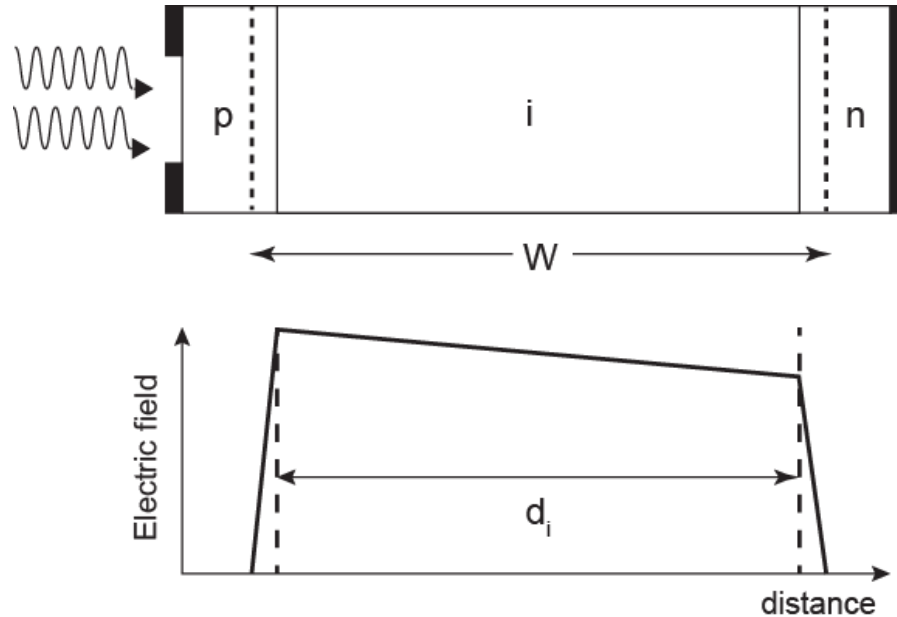
Electrical pulse



# p-i-n photodiode

A layer of undoped (or slightly doped) semiconductor is inserted between the p-n junction :

- Layer is nearly intrinsic,
- Offers high resistance: large electric field exists in the i-layer.



- All absorption takes place in depletion region
- Depletion layer width  $W$  *does not vary* significantly with bias voltage:  $W \approx d_i$
- Optimal value of  $d_i$  depend on *tradeoff between speed and sensitivity*

# Avalanche photodetector

All detectors require a minimum current to operate reliably: have a *minimum power requirement*

$$i_p = RP_{in}$$

Detectors with large responsivity  $R$  are preferred

However responsivity of p-i-n photodiodes are limited and take a maximum value for a quantum efficiency  $\eta = 1$

$$R = \frac{q}{h\nu} \approx \frac{\lambda}{1.24}$$

Avalanche photodiodes (APD) can have much larger  $R$  : they are designed to provide internal current gain

# Avalanche photodetector

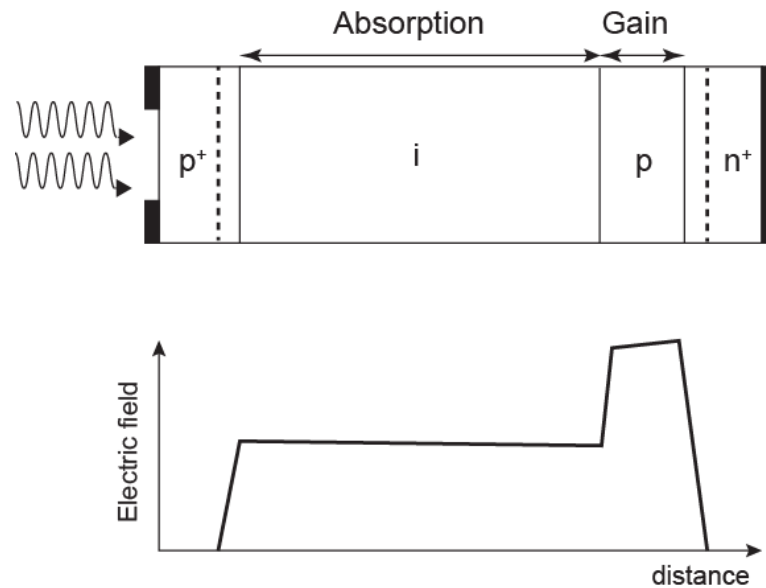
Internal gain of APD is obtained by having a high electric field

- Accelerating electron (hole) can acquire sufficient energy to generate a new electron-hole pair
- These high energy electrons (holes) ionize bound electrons in the valence band upon colliding with them
- Known as impact ionization

Net result of this mechanism

- A primary electron generated through photon absorption creates secondary electrons
- Secondary electrons can also cause further impact ionization: avalanche effect
- All generated electrons contribute to the photodiode current  $i_p$

# APD structure



p-i-n structure with an additional layer

*i* layer still acts as depletion region where most incident photons are absorbed

- Primary electron holes pair

Under reverse bias high  $E$  field exists in the added p-type layer

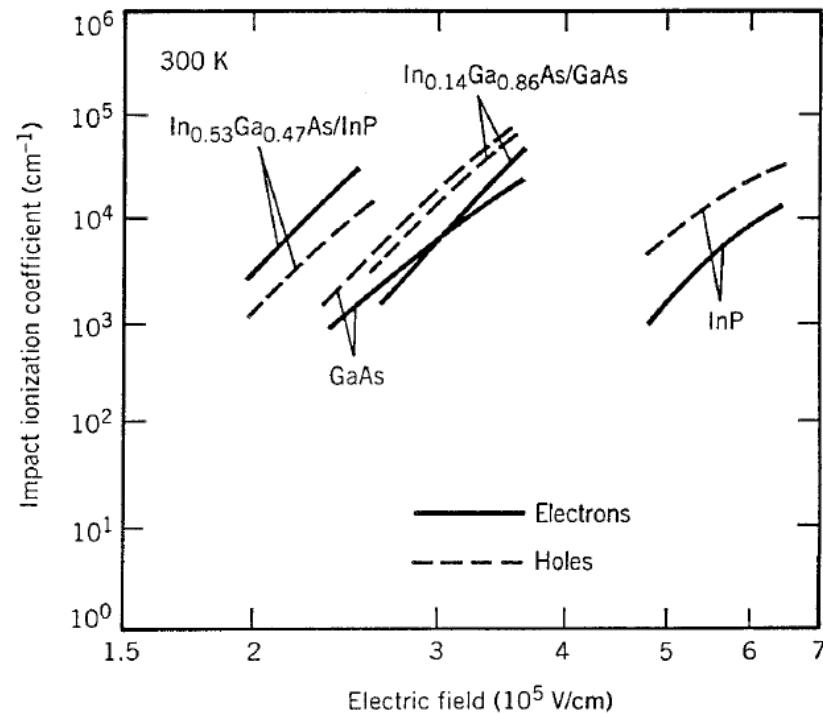
- Secondary electron hole pairs

APDs are characterized by a gain multiplication factor  $M$

$$R_{APD} = MR = M \frac{\eta q}{h\nu}$$

# Impact ionization

Rate of generation is governed by the *impact-ionization coefficients* of electron and hole ( $\alpha_e$ ,  $\alpha_h$ )



Value of  $\alpha_e$ ,  $\alpha_h$  depend on

- Semiconductor material
- Accelerating electric field

Values of  $10^4 \text{ cm}^{-1}$  are obtained for field within the range  $2\text{--}4 \times 10^5 \text{ V/cm}$

- Need voltages near 100 V for APD.

$$k_A \text{ ionization factor} = \begin{cases} \frac{\alpha_h}{\alpha_e} & \text{for } \alpha_h < \alpha_e \\ \frac{\alpha_e}{\alpha_h} & \text{for } \alpha_h > \alpha_e \end{cases}$$

# Average current gain $M$

Rate equations: both electrons and holes produce new electron/hole pairs during the impact ionization

Electron current  $i_e$  :

$$\frac{di_e}{dx} = \alpha_e i_e + \alpha_h i_h$$

Opposite direction hole current  $i_h$  :

$$-\frac{di_h}{dx} = \alpha_e i_e + \alpha_h i_h$$

Total current is:

$$I = i_e(x) + i_h(x)$$



## Average current gain $M$

$$\frac{di_e}{dx} = \alpha_e i_e + \alpha_h (I - i_e) = (\alpha_e - \alpha_h) i_e + \alpha_h I$$

$$\frac{di_e}{dx} + (\alpha_h - \alpha_e) i_e = \alpha_h I$$

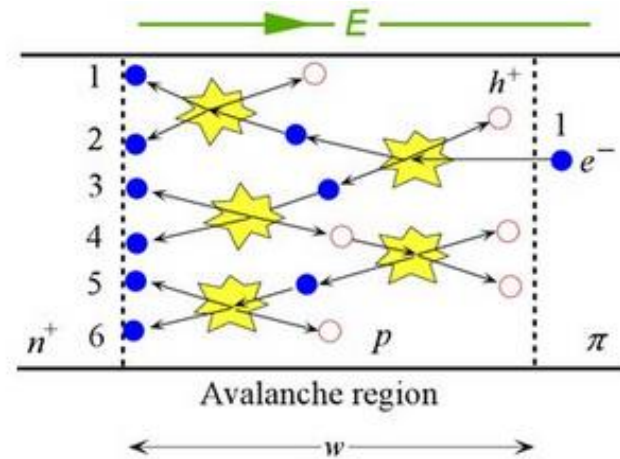
Solution of the form:

$$i_e = \frac{\alpha_h}{(\alpha_h - \alpha_e)} I + k \exp[-(\alpha_h - \alpha_e)x]$$

$k$  determined by boundary condition

Electron current *grows exponentially* when moving into the gain region

# Average current gain $M$



Boundary condition: Only electrons go into the  $n^+$  region:  $i_e(d) = I$  and  $i_h(d) = 0$

Get multiplication factor  $M$ :

$$M = \frac{i_e(d)}{i_e(0)} = \frac{1 - k_A}{\exp[-(1 - k_A)\alpha_e d] - k_A}$$

$$\text{with } k_A = \frac{\alpha_h}{\alpha_e} \text{ for } \alpha_h < \alpha_e$$

## Example

A Si APD has a quantum efficiency of 70% at 830 nm when  $M = 1$ . When illuminated with radiation it produces an output photocurrent of 10  $\mu\text{A}$  after avalanche gain with a multiplication factor of 250.

What is the received optical power to the device ?

How many photons per second does this correspond to ?

# Speed and bandwidth

# Rise time and bandwidth

The photodiode bandwidth is determined by the speed at which the device responds to variations in incident optical power.

Rise time  $T_r$ : time over which the current builds up from 10% to 90% of its final value when incident power is changed abruptly.

Photodetector response time has two components:

- *Transit time of the photocurrent*  $\tau_{tr}$  : time taken by electrons and holes to travel to electrical contacts of photodiode.
- *RC-limited time constant*  $\tau_{RC}$  : response time of the electrical circuit processing the photocurrent.

Note: photodiode operating in photovoltaic mode has large RC constant, only photoconductive diodes are suitable for high speed or broadband applications

# Photo-carrier response time – drift component

Drift of carriers is a fast process

Constant electric field in the depletion region causes the photogenerated carriers to accelerate.

- Motion of carrier is at an average velocity called **drift velocity**  $v_d$

When field in depletion exceeds a saturation value, carriers travel at maximum drift velocity called **saturation velocity**

Longest transit time  $\tau_{tr,drift}$  is when (slowest) carriers traverse entire depletion layer of width  $W$

$$\tau_{tr,drift} = \frac{W}{v_d}$$

# Photo-carrier response time – diffusion component

Carriers generated outside the depletion region but sufficiently close take time to diffuse into it.

- Relatively slow process in comparison with drift.
- Maximum times allowed for this process are the carrier lifetimes.
- Given a diffusion speed of  $v_{diff}$  the diffusion time is:

$$\tau_{diff} = \frac{L_{e/h}}{v_{diff}}$$

Example: hole diffusion through 10 mm of silicon is 40 ns. Electron diffusion time is 8 ns

- For high speed photodiode, this diffusion mechanism has to be eliminated

# RC limited response time

Photodiode has internal resistance  $R_i$  and capacitance  $C_j$

- Under strong reverse bias:  $C_j = \frac{\epsilon_0 \epsilon_r A}{W}$  ( $A$  : area of junction,  $W$ : width)

Other resistances, capacitances or inductances are parasitic and due to contact, packaging or wire connections

- Can be minimized by careful design and packaging.

Frequency response of the equivalent circuit :  $\tau_{RC} \approx R_L C_j$

RC limited 3dB bandwidth:  $\Delta f_{RC} = \frac{1}{2\pi\tau_{RC}}$

Total bandwidth can be approximated by:

$$\Delta f = \frac{1}{[2\pi(\tau_{tr} + \tau_{RC})]}$$



# APD bandwidth

Intrinsic bandwidth also depends on  $M$

- Transit time increases significantly
- For  $\alpha_h \ll \alpha_e$ , effective transit time in the multiplication layer is:

$$\tau_{eff,M} \approx k_A M \tau_{tr,M}$$

$$\text{with } \tau_{tr,M} = \frac{d}{v_d}$$

Assuming  $\tau_{RC} \ll \tau_{eff,M}$  and  $\tau_{tr,i} \ll \tau_{eff,M}$  then :  $\Delta f \approx \frac{1}{2\pi\tau_{eff,M}}$

Tradeoff between gain & bandwidth (speed & sensitivity), better to have  $k_a \ll 1$