

Lecture 8

Photodetectors

EE 440 – Photonic systems and technology
Spring 2025

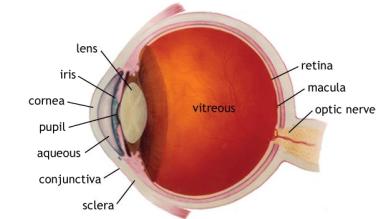
Basic operation principle

Photodetectors convert light (power) into an electrical signal (photocurrent)

- Uses the photoelectric effect.

The eye is a photodetector:

- Spectral response is limited to wavelength of $0.4 \mu\text{m}$ to $0.7 \mu\text{m}$



For telecommunication need:

- Good sensitivity (responsivity) at the desired wavelength of operation.
- Fast response to be able to handle high speed data.
- Low noise to avoid distortions to the signal.
- Compatible physical dimensions with the entire systems
- Long operating life and reasonable cost

Only **photodiodes** are used in optical communication systems

All detectors for optical communication use **optical absorption** in a **depletion region**.

- Light absorption occurs when energy of incident photons exceeds bandgap energy

Photon energy $h\nu >$ Bandgap energy

- Convert photons to electron-hole pairs .
- Can then sense the number of electron-hole pairs generated.

A voltage applied across the device sets an electric field in the depletion region: electron-hole pairs give rise to a measurable photocurrent i_p

- The figure of merit of the photodiode is the responsivity R (in A/W) defined as:

$$i_p = RP_{in}$$

Quantum efficiency

Responsivity of a photodiode can be expressed in terms of the diode's *quantum efficiency* η

$$\eta = \frac{\text{\# electrons from photocurrent generation}}{\text{\# photons incident}}$$

$$\eta = \frac{i_p/q}{P_{in}/h\nu} = \frac{h\nu}{q} \frac{i_p}{P_{in}} = \frac{h\nu}{q} R \quad \text{With } q = \text{electronic charge}$$

Rewrite responsivity:

$$R = \frac{\eta q}{h\nu}$$

$$R \approx \frac{\eta \lambda}{1.24}, \lambda \text{ in } \mu\text{m}$$

Responsivity

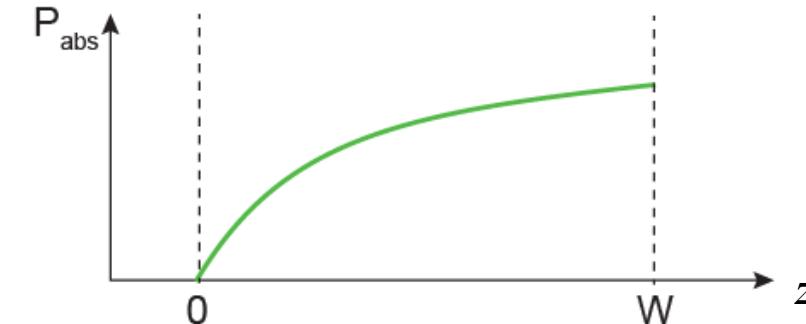
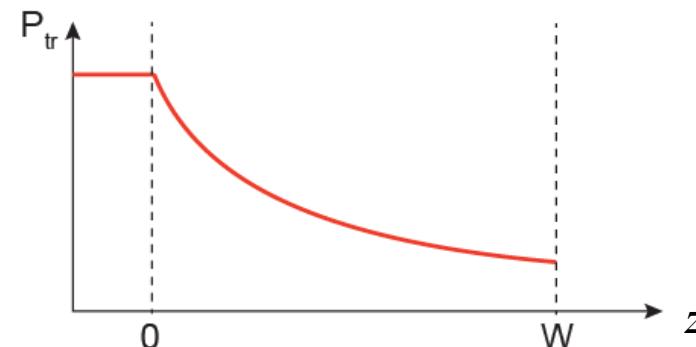
Absorption coefficient

As the photon flux goes through the semiconductor of thickness W , it will be absorbed as it progresses through the material.

- Given absorption coefficient α , transmitted (P_{tr}) and absorbed powers (P_{abs}) are:

$$P_{tr}(z) = P_{in} \exp(-\alpha z)$$

$$P_{abs}(z) = P_{in} - P_{tr}(z) = P_{in}[1 - \exp(-\alpha z)]$$



Quantum efficiency

Since each absorbed photon creates an electron-hole pair we define an absorption quantum efficiency:

$$\eta_{abs} = \frac{P_{abs}(W)}{P_{in}(W)} = 1 - \exp(-\alpha W)$$

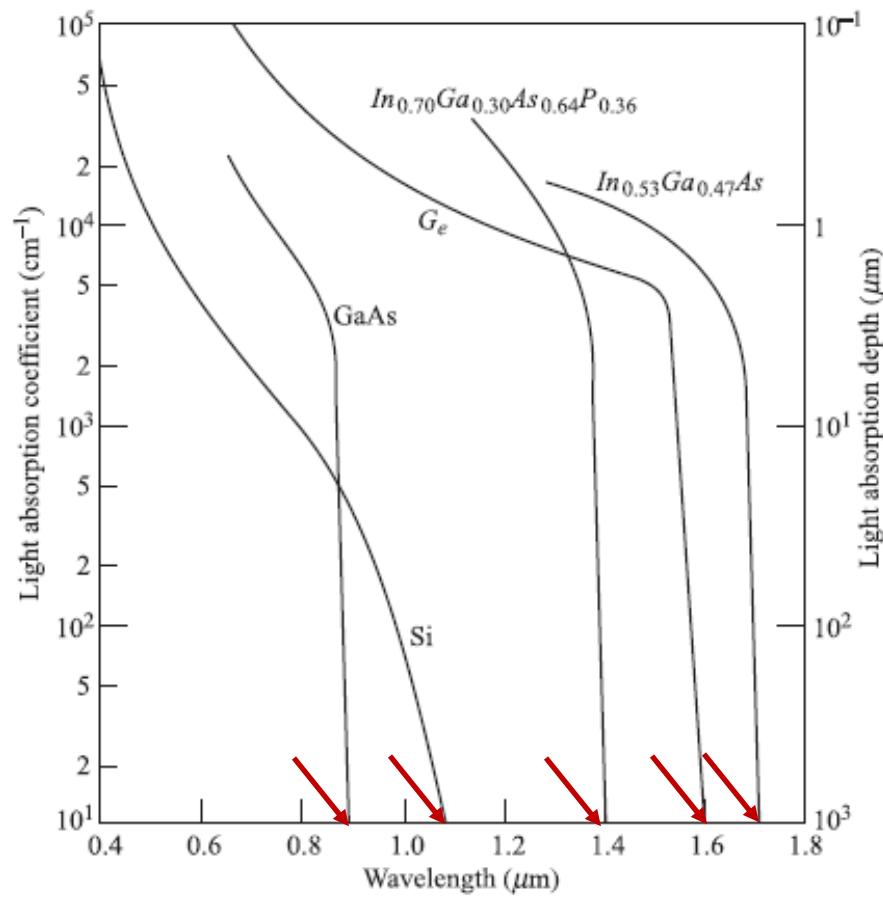
Photodiodes also have an internal quantum efficiency η_{int}

- Not all electron-hole pairs will contribute to the photocurrent.

The quantum efficiency is therefore given by:

$$\eta = \eta_{int} \eta_{abs} = \eta_{int} [1 - \exp(-\alpha W)]$$

Absorption coefficient α



Large values of α (10^4 cm^{-1}) can be realized in most semiconductors

Photodetectors can be made of indirect bandgap semiconductor (Si, Ge)

- Absorption edge is not as sharp

Absorption becomes tends to zero at the cut-off wavelength λ_c

$$\lambda_c = \frac{hc}{E_g}$$

Example

A photodiode has a quantum efficiency of 50% at a wavelength of 900 nm.

What is its responsivity at 900 nm ?

What is the optical power if the mean photocurrent is 10 μ A?

Given that the absorption is 10^3 cm^{-1} , and assume 100% internal quantum efficiency, what is the length of the active medium ?

Types of photodiodes

Photodiode types

p-n photodiodes

- Electron-hole pairs created in the depletion region of a p-n junction in proportion to the optical power
- Electrons and holes are swept out by the electric field leading to a current (in photoconductive mode)

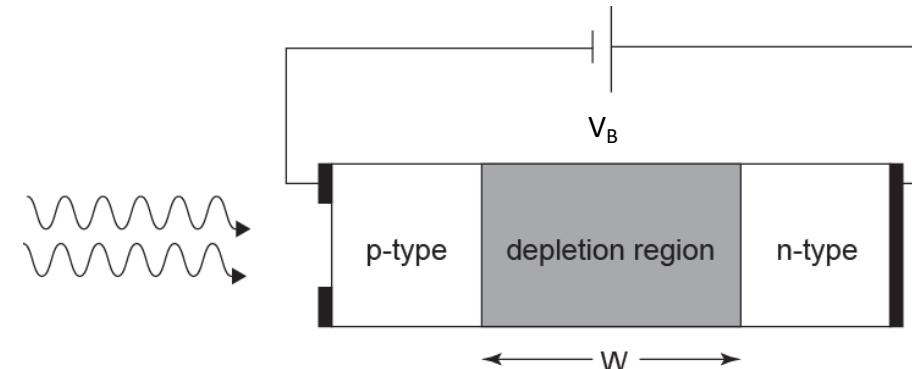
p-i-n photodiodes

- Electric field is concentrated in an intrinsic (i) layer

Avalanche photodiodes (APD)

- Like p-i-n photodiodes but have an additional layer
- An average of M secondary electron-hole pairs are generated through impact ionization for each primary pair

A p-n photodiode is a p-n junction whose reverse current increases when it absorbs photon



Photons are absorbed everywhere with absorption coefficient α , is resulting in electron-hole pairs

Under an electric field the generated charge carriers can be transported

- For a p-n junction, electric field is only in the depletion region
- The depletion region is therefore where it is desirable to generate photo-carriers.

Bias of p-n photodiode

As an electronic device, the photodiode under illumination has an $i - V$ relation given by:

$$i = i_0 \left[\exp \left(\frac{qV}{k_B T} \right) - 1 \right] - i_p$$

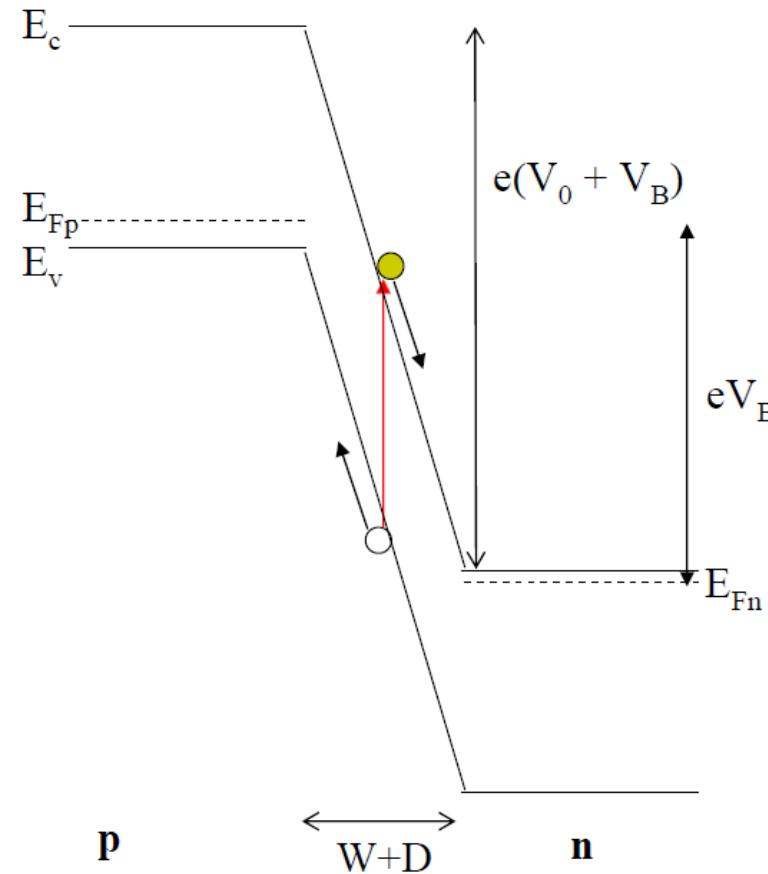
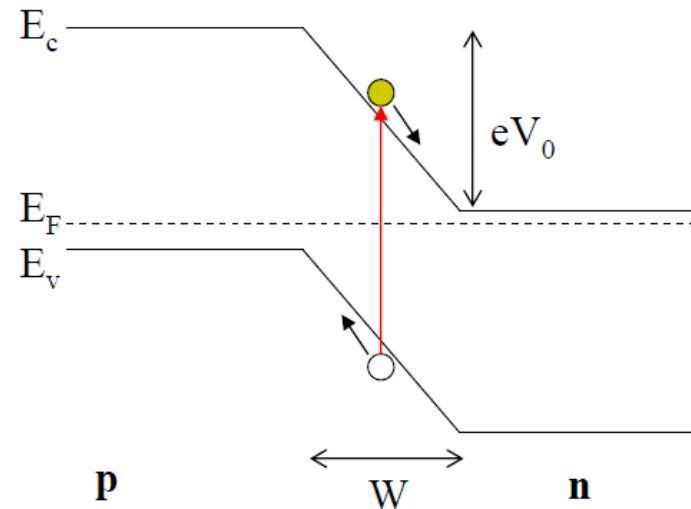
i : is the injection current under a forward bias V

i_0 : is the dark current representing thermal generated free carrier which flow through the junction

There are two modes of operation for a junction photodiode

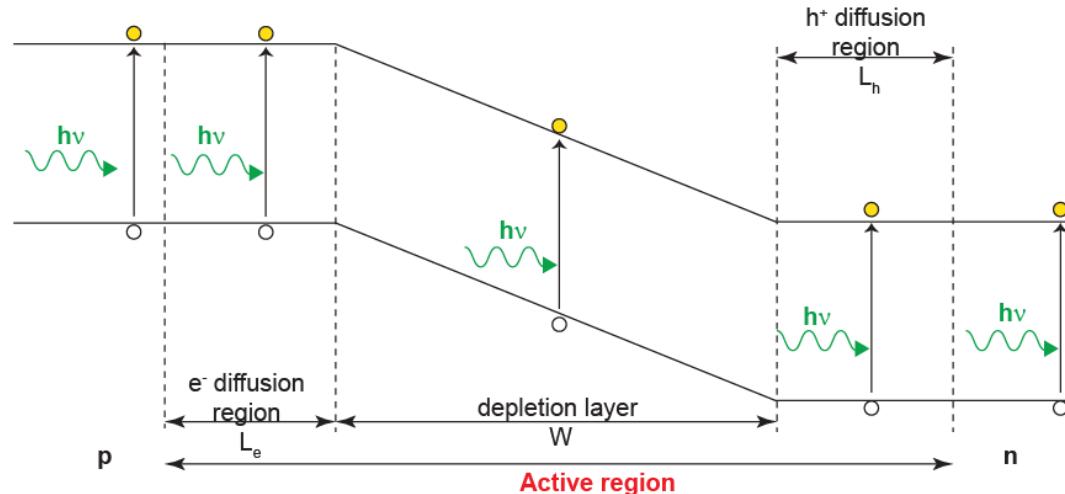
- Photoconductive mode – including short circuit condition (current source)
- Photovoltaic mode – including open circuit condition (voltage source)

Reverse bias p-n junction



Reverse biased mode: photoconductive

e^- - h pairs can be generated in *3 possible locations*



Depletion region

Charges quickly drift in opposite directions under influence of strong E field and *contribute* to the reverse photocurrent i_p

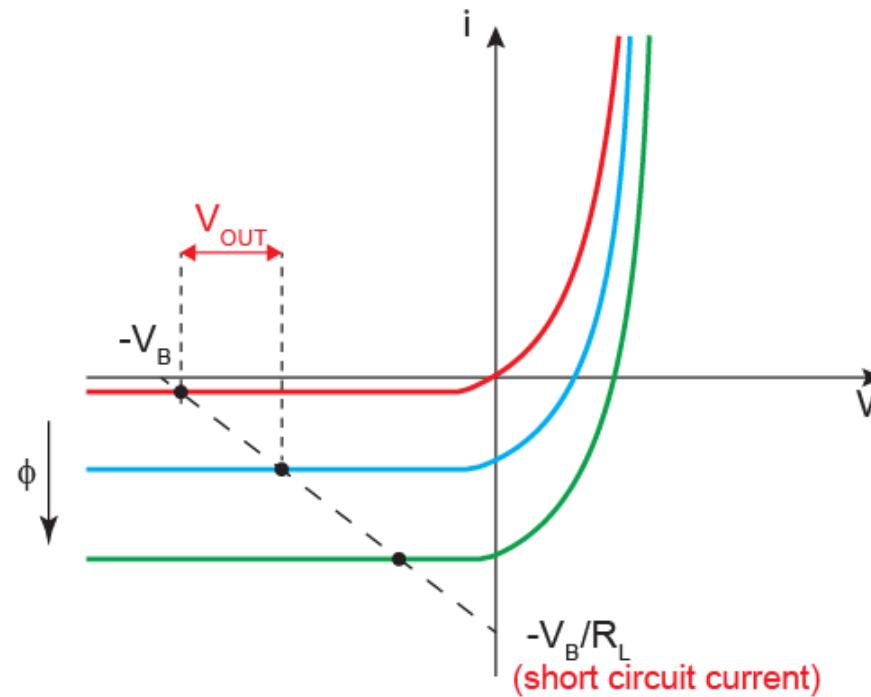
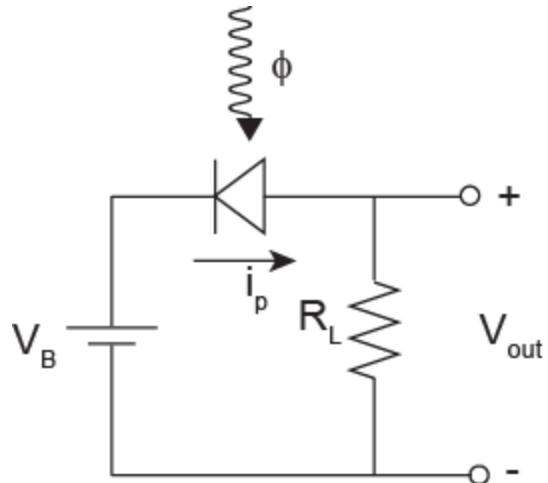
Away from depletion region

Charged cannot be transported (no E field): wander until recombined, not contributing to the photocurrent i_p

Vicinity of depletion region

Charges can enter depletion region by random diffusion and then *contribute* to the reverse photocurrent i_p

Reverse biased mode: photoconductive

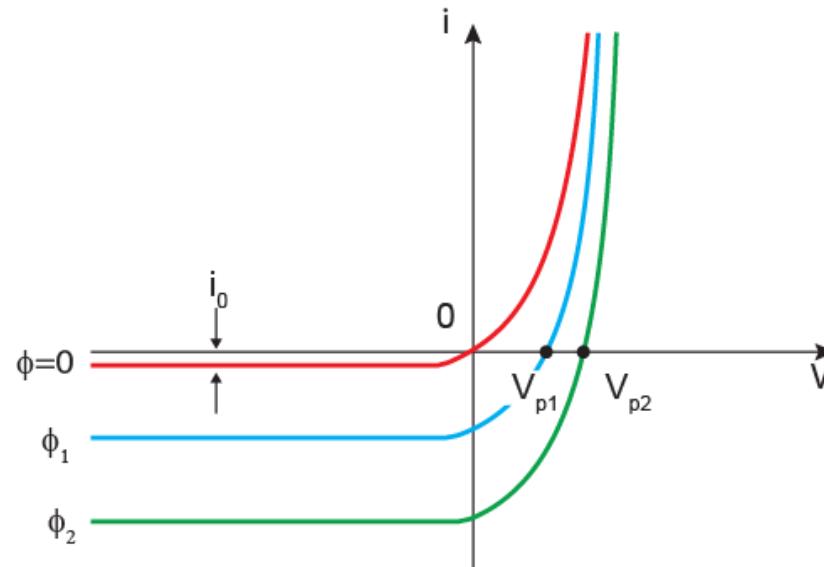
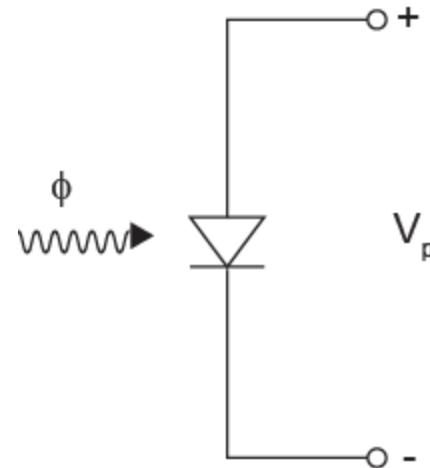


Load resistor R_L is inserted in the circuit

- $R_L < R_i$, the internal resistance of the junction
- Keep $V_{out} < V_B$ so that the diode remains reversed biased

Have $V_{out} = (i_0 + i_p)R_L$

Open circuit mode: photovoltaic



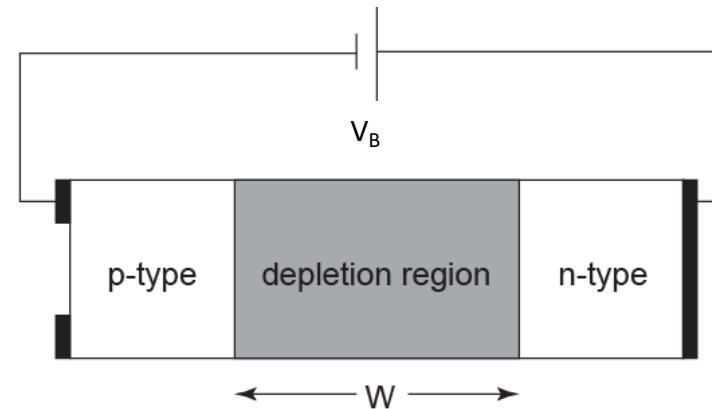
Light generates e^- - h pairs in depletion region

- Photogenerated majority carriers *forward bias* the junction
- Net result: *photovoltage* V_p across the device

Limit on V_p is the equilibrium contact potential V_0 as drift current vanishes with $V_p = V_0$

Note: responsivity for such device is measured in V/W rather than A/W

Limits of p-n photodiodes



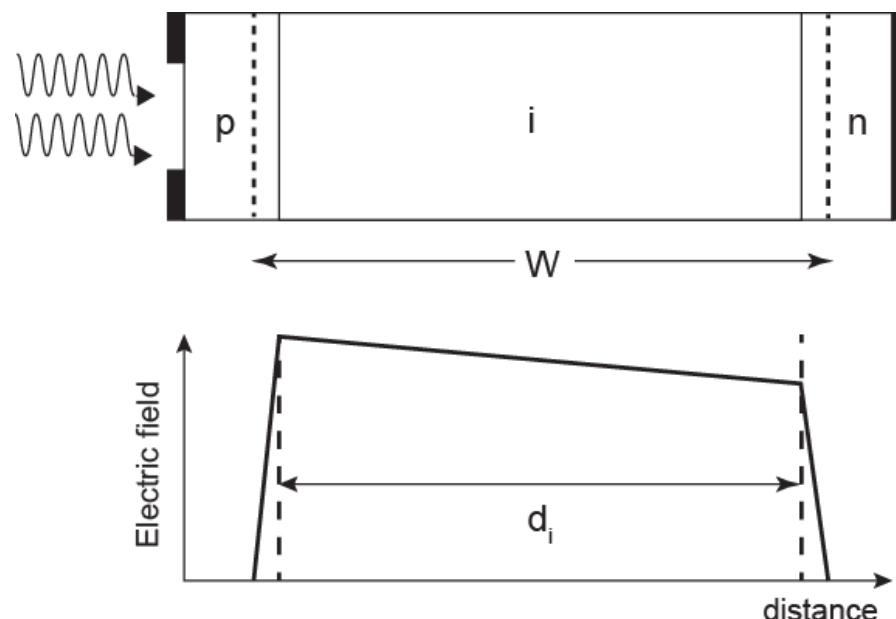
Problem with p-n photodiode is the limited width of depletion region:

- Leads to the presence of a diffusive component in the photocurrent.
- Diffusion is slow process ($>$ ns to diffuse $1\mu\text{m}$): distorts response of photodiode.



A layer of undoped (or slightly doped) semiconductor is inserted between the p-n junction :

- Layer is nearly intrinsic,
- Offers high resistance: large electric field exists in the i-layer.



- All absorption takes place in depletion region
- Depletion layer width W *does not vary* significantly with bias voltage: $W \approx d_i$
- Optimal value of d_i depend on *tradeoff between speed and sensitivity*

All detectors require a minimum current to operate reliably: have a *minimum power requirement*

$$i_p = RP_{in}$$

Detectors with large responsivity R are preferred

However responsivity of p-i-n photodiodes are limited and take a maximum value for a quantum efficiency $\eta = 1$

$$R = \frac{q}{h\nu} \approx \frac{\lambda}{1.24}$$

Avalanche photodiodes (APD) can have much larger R : they are designed to provide internal current gain

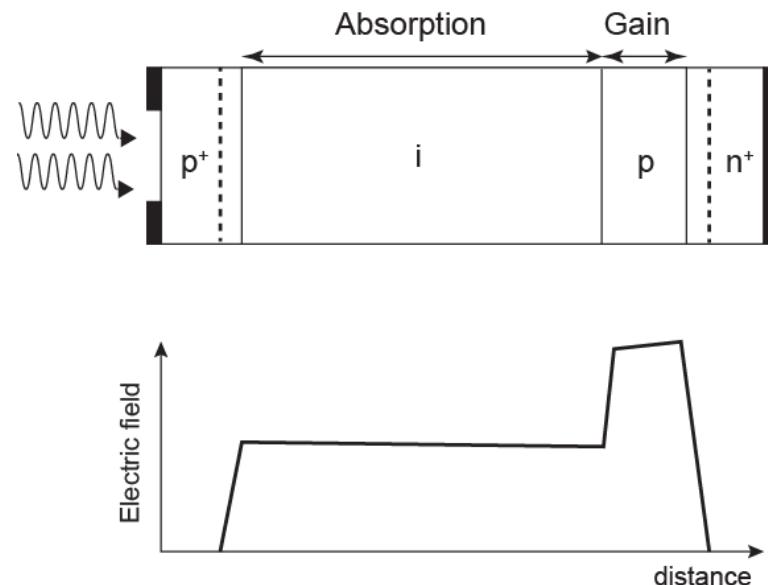
Internal gain of APD is obtained by having a high electric field

- Accelerating electron (hole) can acquire sufficient energy to generate a new electron-hole pair
- These high energy electrons (holes) ionize bound electrons in the valence band upon colliding with them
- Known as impact ionization

Net result of this mechanism

- A primary electron generated through photon absorption creates secondary electrons
- Secondary electrons can also cause further impact ionization: avalanche effect
- All generated electrons contribute to the photodiode current i_p

APD structure



p-i-n structure with an additional layer

i layer still acts as depletion region where most incident photons are absorbed

- Primary electron holes pair

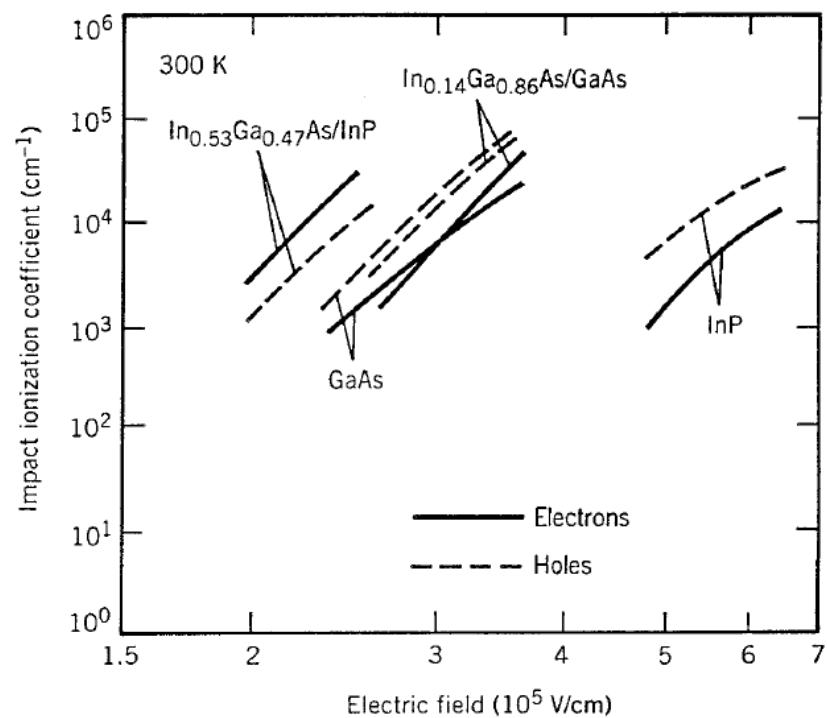
Under reverse bias high *E* field exists in the added p-type layer

- Secondary electron hole pairs

APDs are characterized by a gain multiplication factor M

$$R_{APD} = MR = M \frac{\eta q}{h\nu}$$

Rate of generation is governed by the *impact-ionization coefficients* of electron and hole (α_e , α_h)



Value of α_e , α_h depend on

- Semiconductor material
- Accelerating electric field

Values of 10^4 cm^{-1} are obtained for field within the range $2-4 \times 10^5 \text{ V/cm}$

- Need voltages near 100 V for APD.

$$k_A \text{ ionization factor} = \begin{cases} \frac{\alpha_h}{\alpha_e} & \text{for } \alpha_h < \alpha_e \\ \frac{\alpha_e}{\alpha_h} & \text{for } \alpha_h > \alpha_e \end{cases}$$

Average current gain M

Rate equations: both electrons and holes produce new electron/hole pairs during the impact ionization

Electron current i_e :

$$\frac{di_e}{dx} = \alpha_e i_e + \alpha_h i_h$$

Opposite direction hole current i_h : $-\frac{di_h}{dx} = \alpha_e i_e + \alpha_h i_h$

Total current is:

$$I = i_e(x) + i_h(x)$$

Average current gain M

$$\frac{di_e}{dx} = \alpha_e i_e + \alpha_h (I - i_e) = (\alpha_e - \alpha_h) i_e + \alpha_h I$$

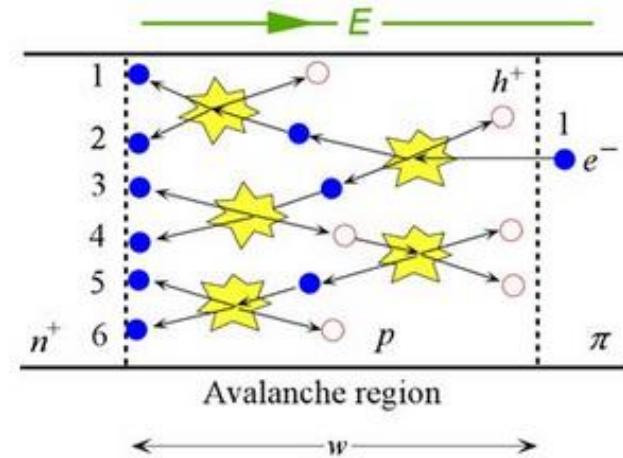
$$\frac{di_e}{dx} + (\alpha_h - \alpha_e) i_e = \alpha_h I$$

Solution of the form: $i_e = \frac{\alpha_h}{(\alpha_h - \alpha_e)} I + k \exp[-(\alpha_h - \alpha_e)x]$

k determined by boundary condition

Electron current *grows exponentially* when moving into the gain region

Average current gain M



Boundary condition: Only electrons go into the n^+ region: $i_e(d) = I$ and $i_h(d) = 0$

Get multiplication factor M:

$$M = \frac{i_e(d)}{i_e(0)} = \frac{1 - k_A}{\exp[-(1 - k_A)\alpha_e d] - k_A}$$

$$\text{with } k_A = \frac{\alpha_h}{\alpha_e} \text{ for } \alpha_h < \alpha_e$$

Example

A Si APD has a quantum efficiency of 70% at 830 nm when $M = 1$. When illuminated with radiation it produces an output photocurrent of 10 uA after avalanche gain with a multiplication factor of 250.

What is the received optical power to the device ?

How many photons per second does this correspond to ?

Speed and bandwidth

Rise time and bandwidth

The photodiode bandwidth is determined by the speed at which the device responds to variations in incident optical power.

Rise time T_r : time over which the current builds up from 10% to 90% of its final value when incident power is changed abruptly.

Photodetector response time has two components:

- *Transit time of the photocurrent* τ_{tr} : time taken by electrons and holes to travel to electrical contacts of photodiode.
- *RC-limited time constant* τ_{RC} : response time of the electrical circuit processing the photocurrent.

Note: photodiode operating in photovoltaic mode has large RC constant, only photoconductive diodes are suitable for high speed or broadband applications

Photo-carrier response time – drift component

Drift of carriers is a fast process

Constant electric field in the depletion region causes the photogenerated carriers to accelerate.

- Motion of carrier is at an average velocity called **drift velocity** v_d

When field in depletion exceeds a saturation value, carriers travel at maximum drift velocity called **saturation velocity**

Longest transit time $\tau_{tr,drift}$ is when (slowest) carriers traverse entire depletion layer of width W

$$\tau_{tr,drift} = \frac{W}{v_d}$$

Photo-carrier response time – diffusion component

Carriers generated outside the depletion region but sufficiently close take time to diffuse into it.

- Relatively slow process in comparison with drift.
- Maximum times allowed for this process are the carrier lifetimes.
- Given a diffusion speed of v_{diff} the diffusion time is:

$$\tau_{diff} = \frac{L_{e/h}}{v_{diff}}$$

Example: hole diffusion through 10 mm of silicon is 40 ns. Electron diffusion time is 8 ns

- For high speed photodiode, this diffusion mechanism has to be eliminated

RC limited response time

Photodiode has internal resistance R_i and capacitance C_j

- Under strong reverse bias: $C_j = \frac{\varepsilon_0 \varepsilon_r A}{W}$ (A : area of junction, W : width)

Other resistances, capacitances or inductances are parasitic and due to contact, packaging or wire connections

- Can be minimized by careful design and packaging.

Frequency response of the equivalent circuit : $\tau_{RC} \approx R_L C_j$

RC limited 3dB bandwidth: $\Delta f_{RC} = \frac{1}{2\pi\tau_{RC}}$

Total bandwidth can be approximated by:

$$\Delta f = \frac{1}{[2\pi(\tau_{tr} + \tau_{RC})]}$$

APD bandwidth

Intrinsic bandwidth also depends on M

- Transit time increases significantly
- For $\alpha_h \ll \alpha_e$, effective transit time in the multiplication layer is:

$$\tau_{eff,M} \approx k_A M \tau_{tr,M}$$

$$\text{with } \tau_{tr,M} = \frac{d}{v_d}$$

Assuming $\tau_{RC} \ll \tau_{eff,M}$ and $\tau_{tr,i} \ll \tau_{eff,M}$ then : $\Delta f \approx \frac{1}{2\pi\tau_{eff,M}}$

Tradeoff between gain & bandwidth (speed & sensitivity), better to have $k_a \ll 1$